

# Current Status of $\pi^+\pi^0\gamma$ analysis

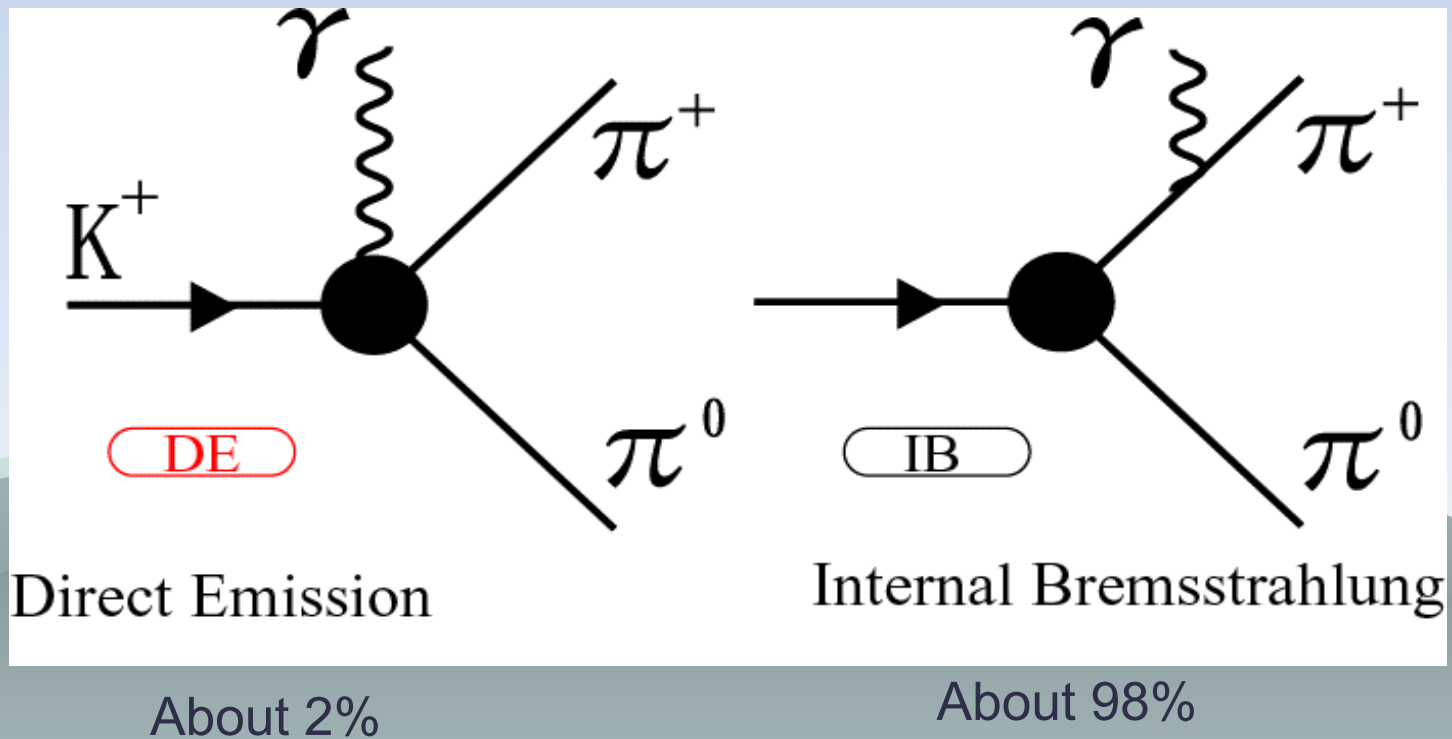
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Toshinao Tsunemi

## Outline

1. Theory
2. Kinetic region in this analysis
3. correction on target
4. consistency between real data and UMC
5. summary

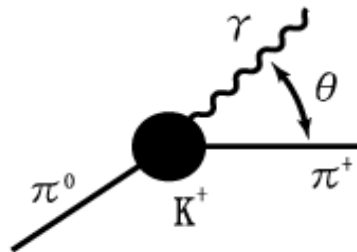
# IB and DE component



# Spectrum for IB and DE separation

$$\frac{\partial^2 \Gamma}{\partial T_+ \partial W} = \frac{\partial^2 \Gamma_{IB}}{\partial T_+ \partial W} \overset{\text{IB}}{(1 + 2 \frac{m_{\pi^+}^2}{m_K^2} \overset{\text{INT}}{Re}(\frac{E}{eA}) W^2} + \overset{\text{DE}}{\frac{m_{\pi^+}^2}{m_K^2} (|\frac{E}{eA}|^2 + |\frac{M}{eA}|^2) W^4)}$$

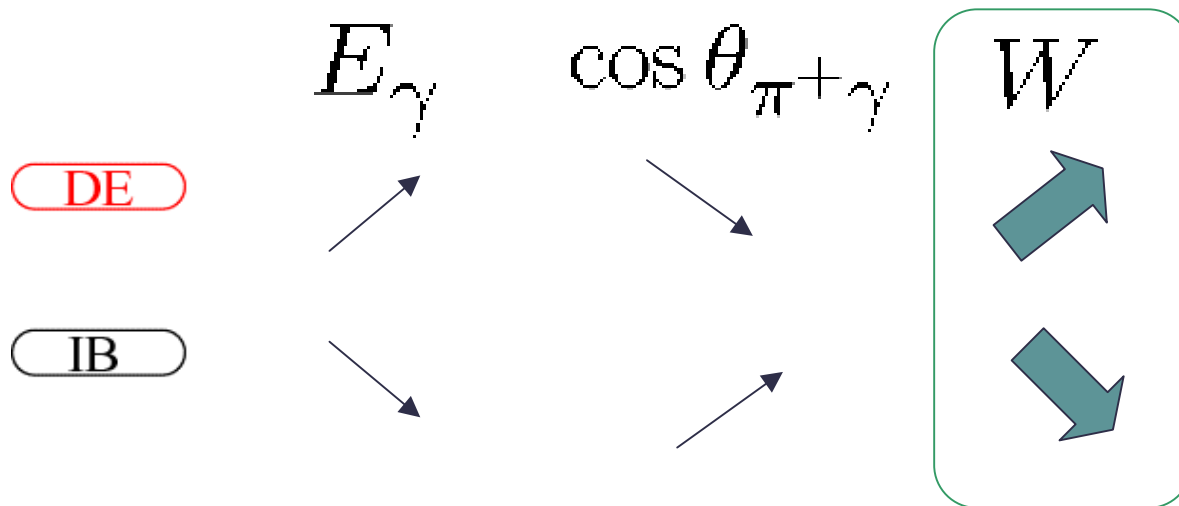
$$W^2 = \frac{E_\gamma^2 \times (E_{\pi^+} - P_{\pi^+} \times \cos \theta_{\pi^+ \gamma})}{m_{K^+} \times m_{\pi^+}^2}$$



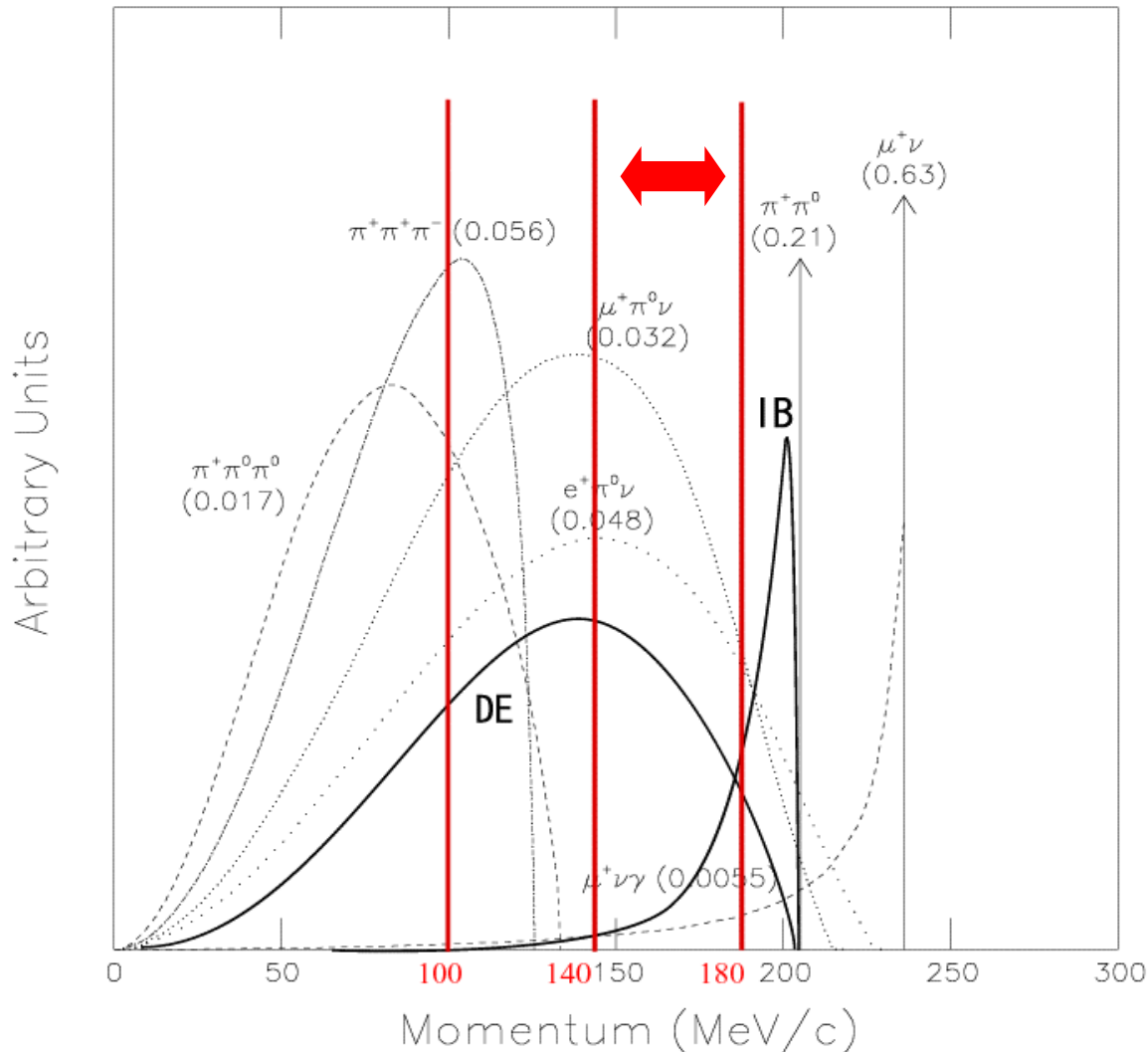
|             |                       |                              |                                      |
|-------------|-----------------------|------------------------------|--------------------------------------|
| $E_\gamma$  | radiated gamma energy | $\cos \theta_{\pi^+ \gamma}$ | opening angle between pion and gamma |
| $E_{\pi^+}$ | pion energy           | $m_{K^+}$                    | kaon mass                            |
| $P_{\pi^+}$ | pion momentum         | $m_{\pi^+}$                  | pion mass                            |

# W spectrum

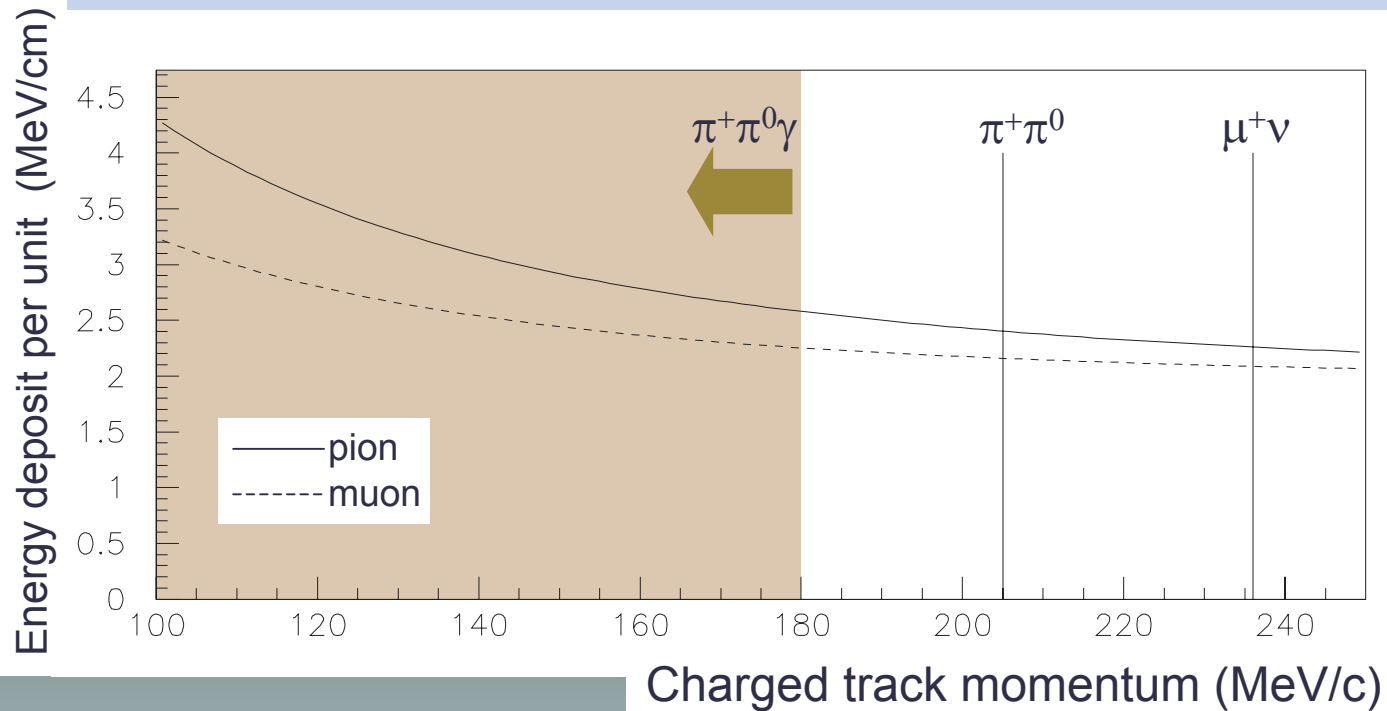
$$W^2 = \frac{E_\gamma^2 \times (E_{\pi^+} - P_{\pi^+} \times \cos \theta_{\pi^+\gamma})}{m_{K^+} \times m_{\pi^+}^2}$$



# Charged track spectrum



# $dE/dx$ in scintillator



$dE/dX$  is large



TARGET plays more important role

# Correction on target

- ◆ Azimuthal angle of charged track
- ◆ Range in target
- ◆ Energy deposit in target



Study with UMC was performed

UMC provides us true value of the measured variables.

# Azimuthal angle

E787 standard extrapolate the UTC track, assuming that the track in target is a part of circle. This means energy deposit in target is neglected.

## New method

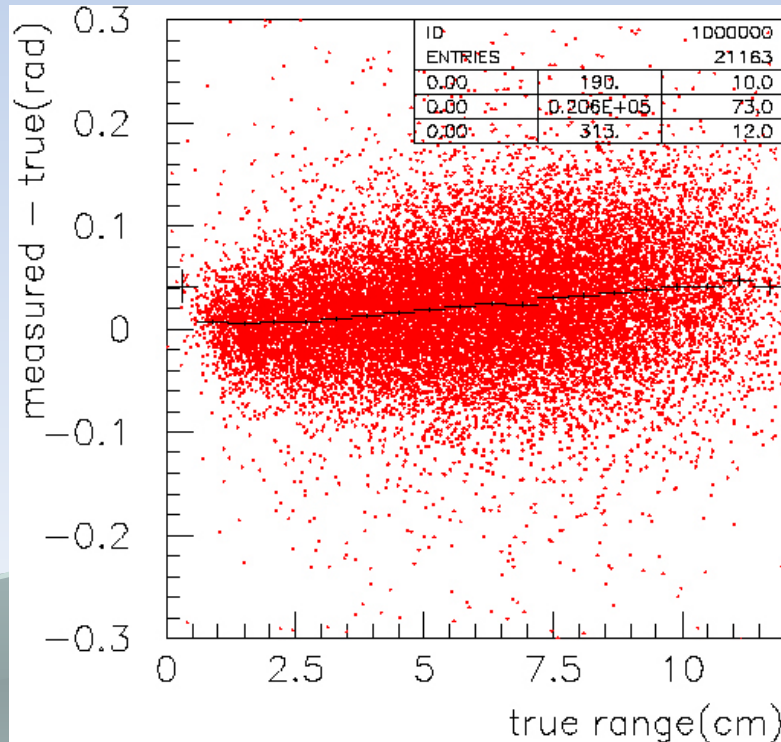
Step by step extrapolation. Energy deposit is calculated, being based on Bethe-bloch formula.

Pion cell

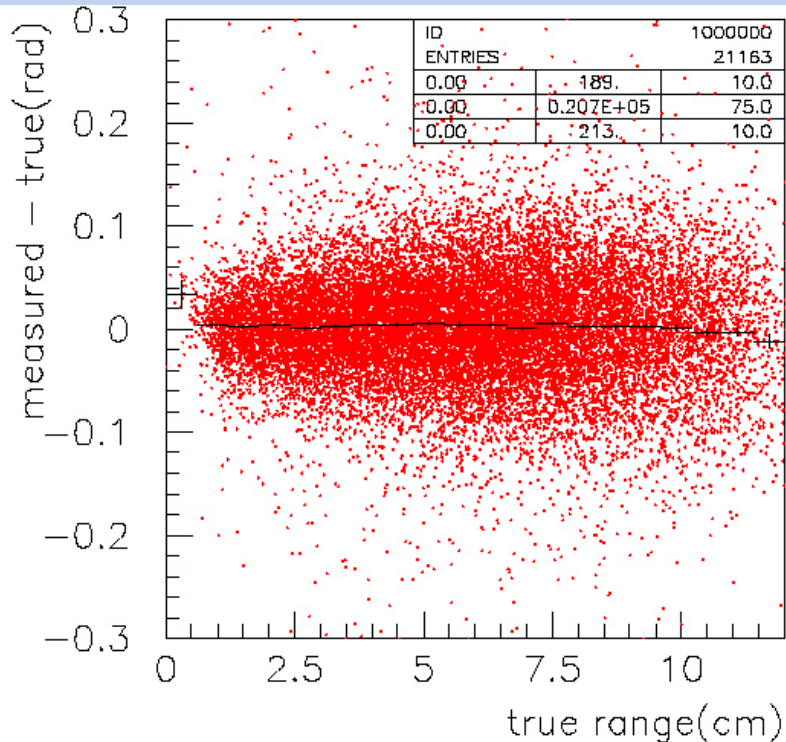
— Simple extrapolation  
— True track



# Azimuthal angle



E787 standard  
Energy deposit in target is  
neglected.

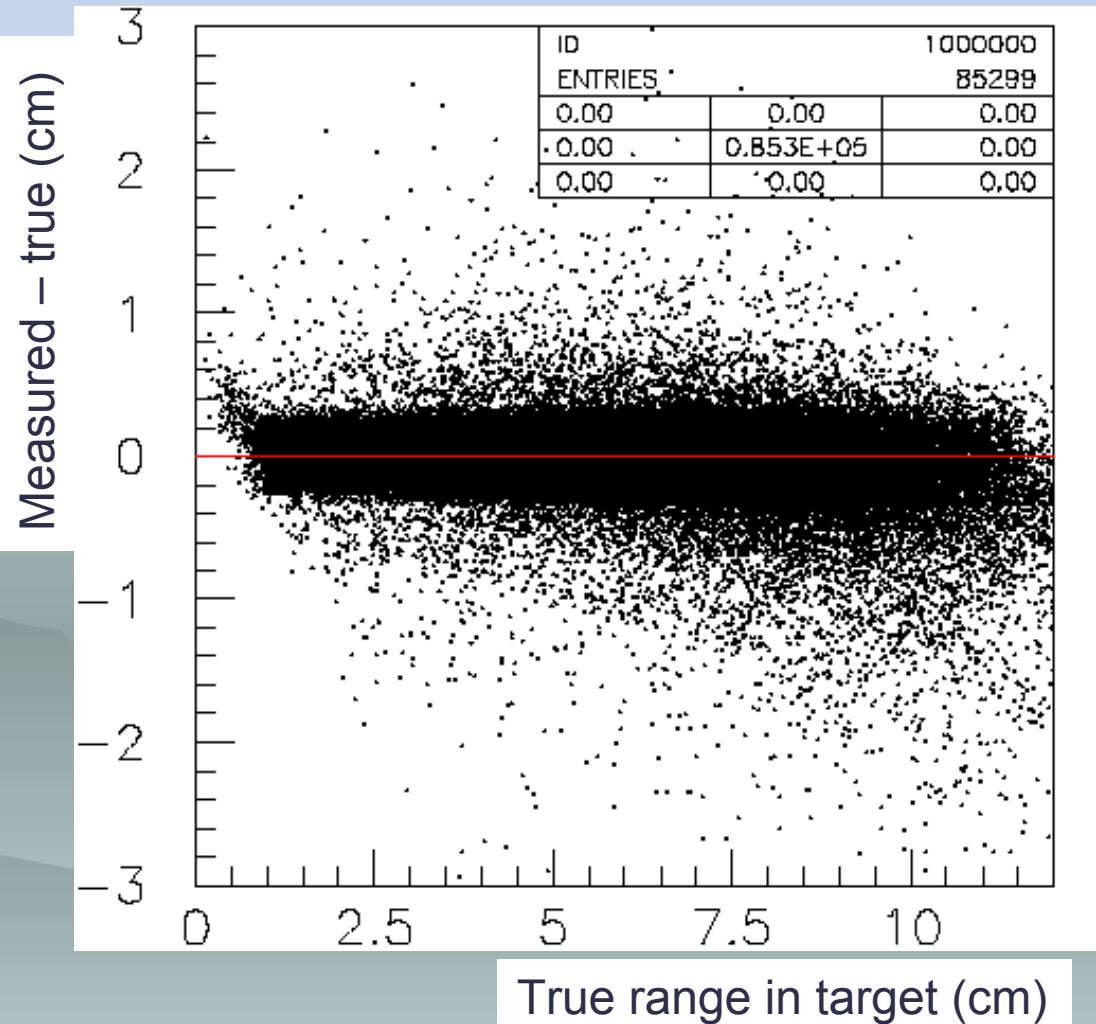


New method.  
Energy deposit is  
calculated, being based on  
Bethe-Bloch formula.

Resolution of azimuthal angle for kinetic fitting is estimated well

# Range in target

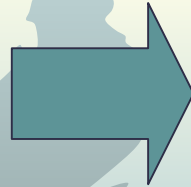
B4-SWATH mode in target reconstruction did not work. It is fixed.



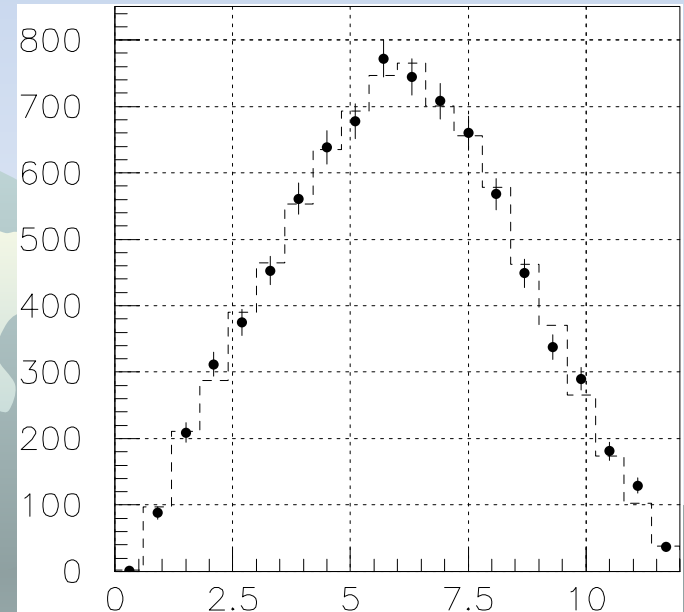
# range in target

- Real
- UMC

previous



new



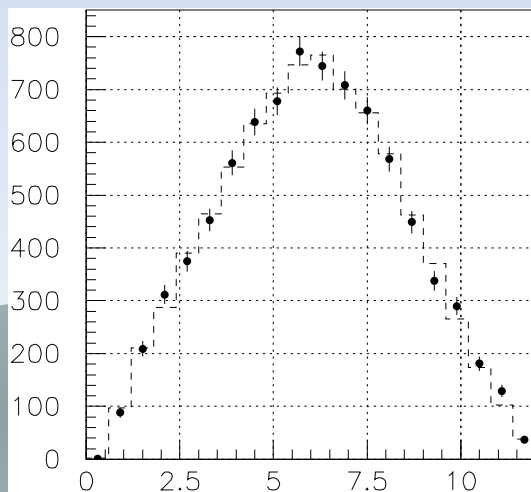
Range in target (cm)

Range in target (cm)

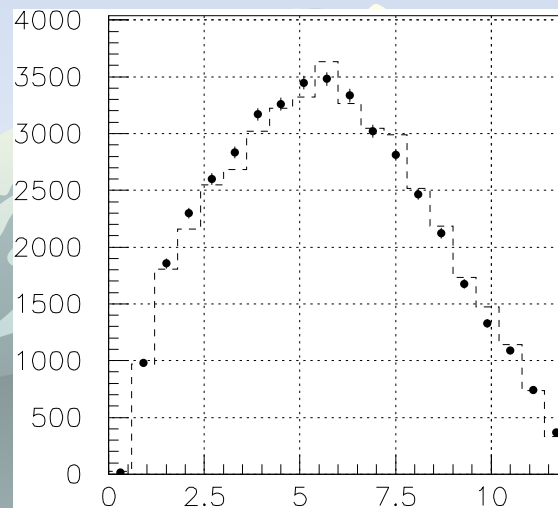
(normalized by number of events)

# Range in target (cm)

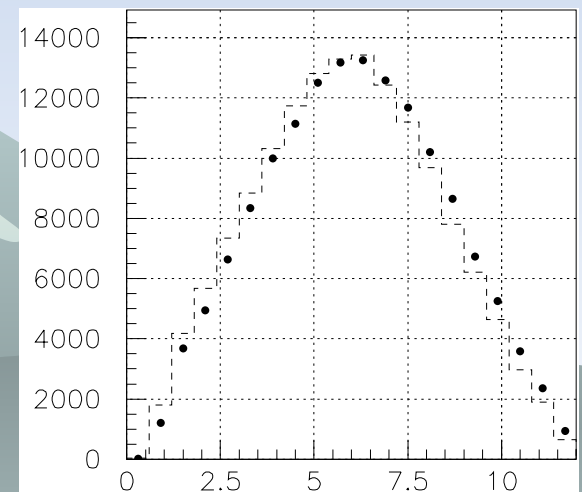
- Real
- UMC



$\pi^+\pi^0\gamma$



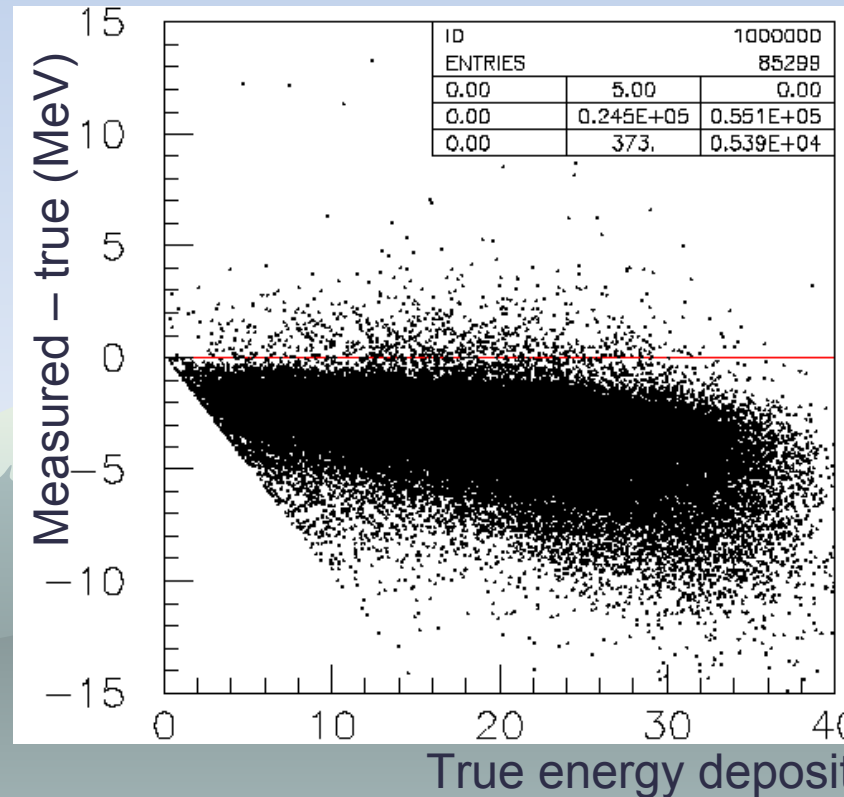
$\pi^+\pi^0$



$\mu^+\nu$

Consistency between real and UMC is retained

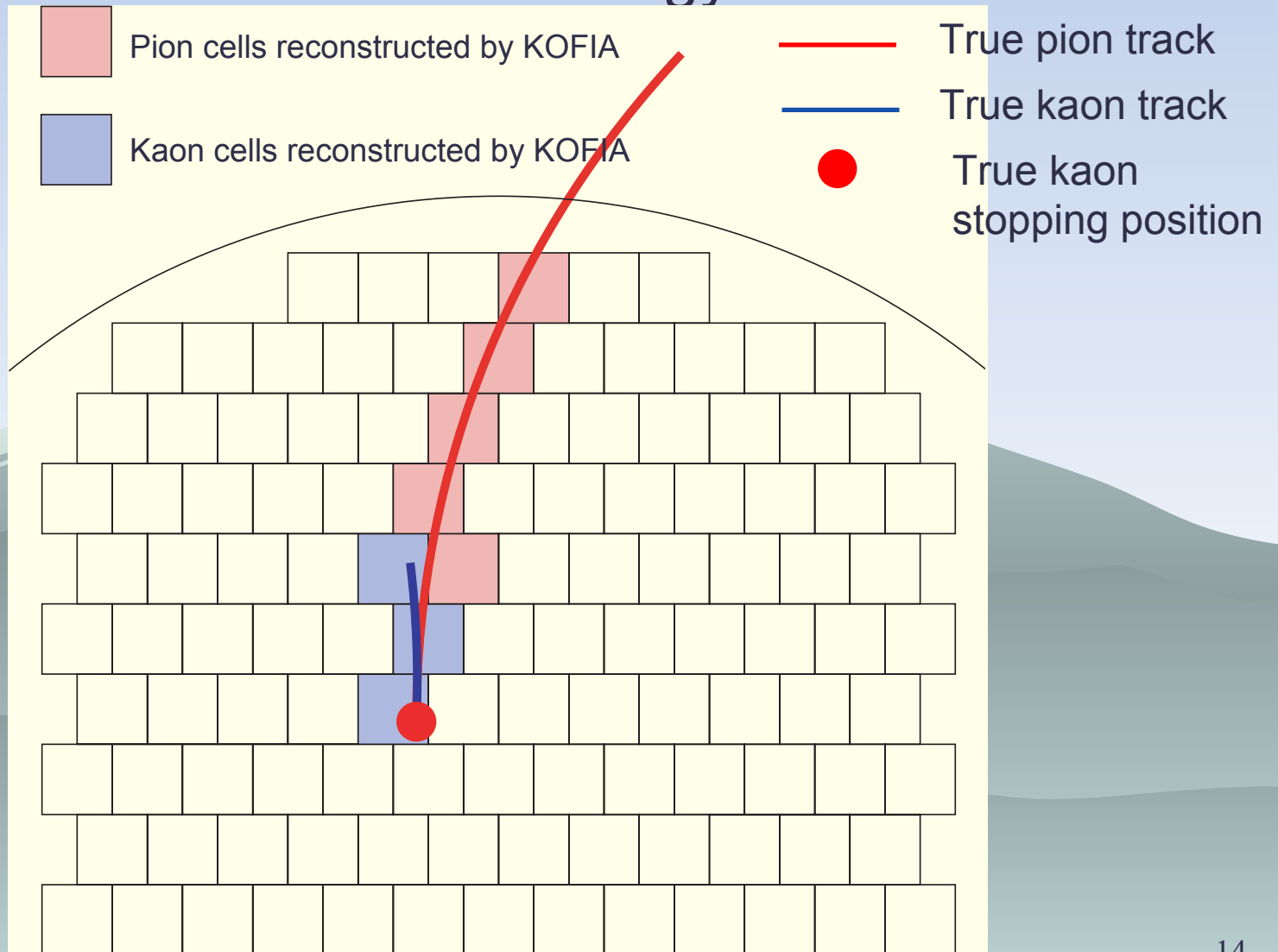
# Energy deposit in target



- ◆ Hidden energy
- ◆ Energy deposit in edge fiber
- ◆ Saturation effect

# Energy deposit in target

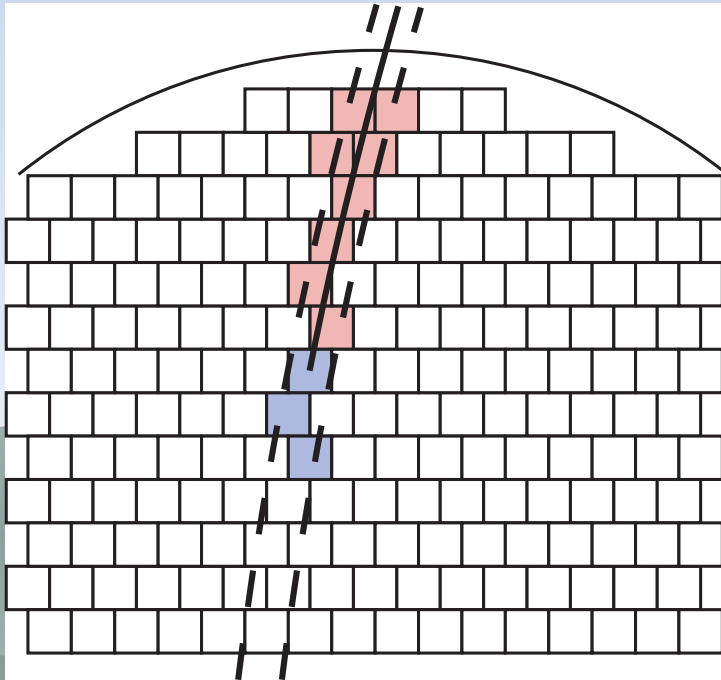
## Hidden Energy



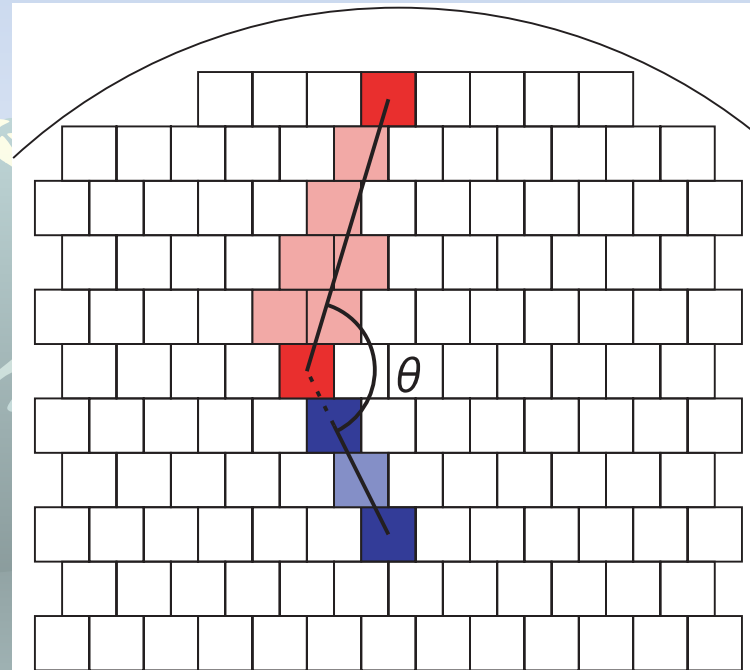
# Energy deposit in target

## Hidden energy

Two measurable variables are used for correction



Number of kaon cells in swath



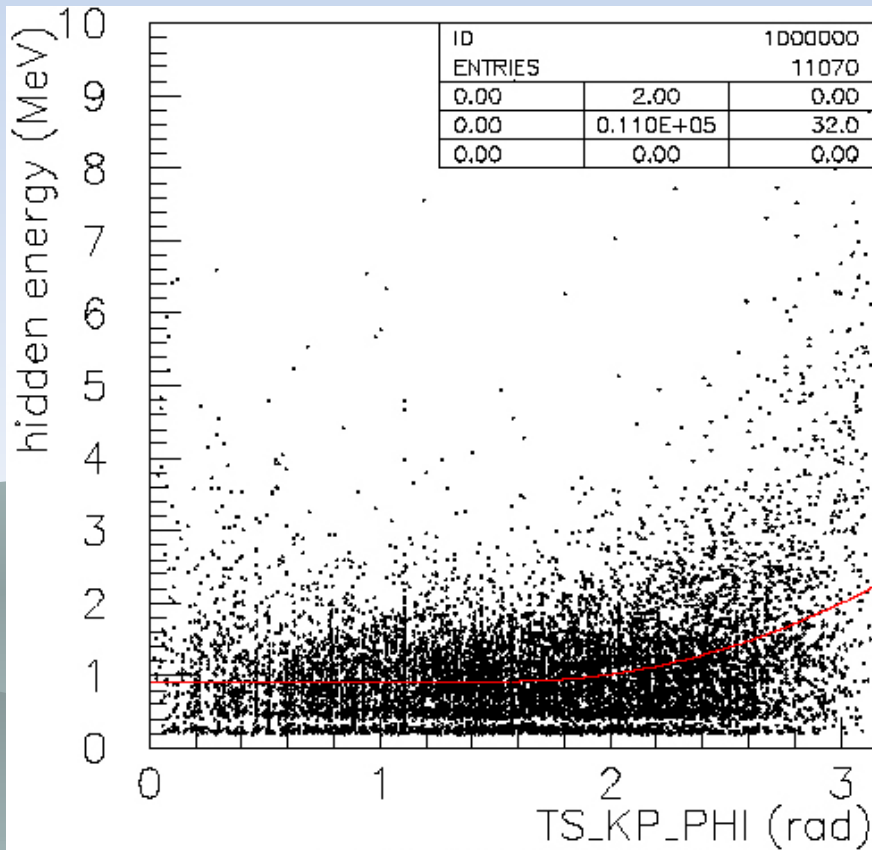
Angle between kaon and pion

Hidden energy depends on two variables

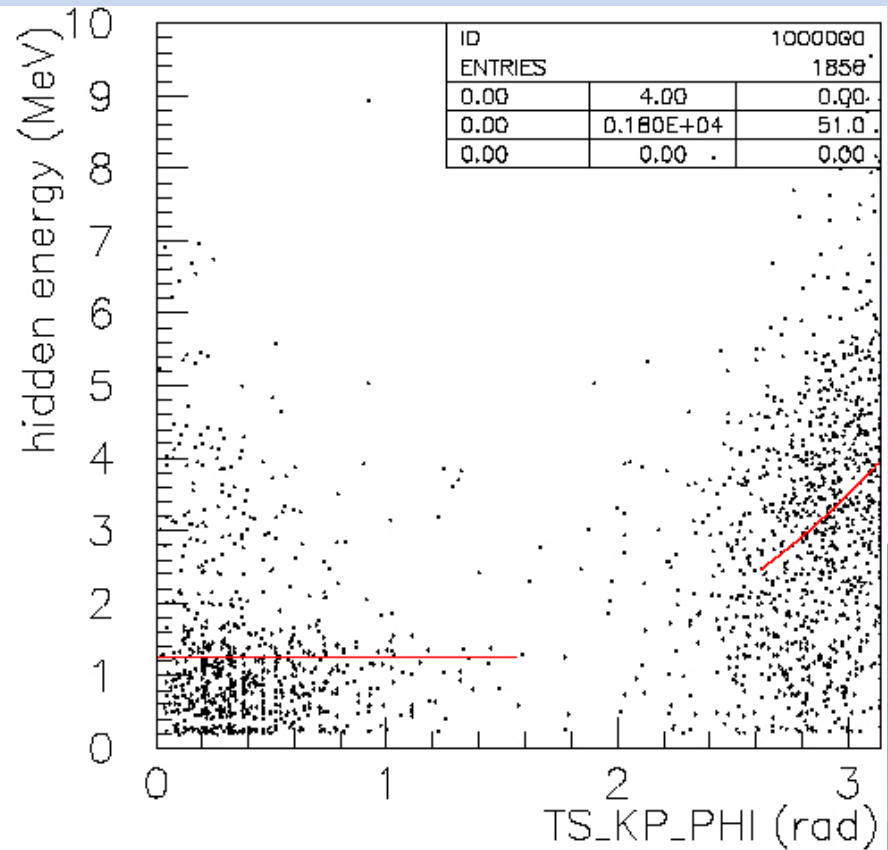
# Energy deposit in target

## Hidden energy

Angle between kaon and pion vs. hidden energy



Number of kaon cells in swath= 1



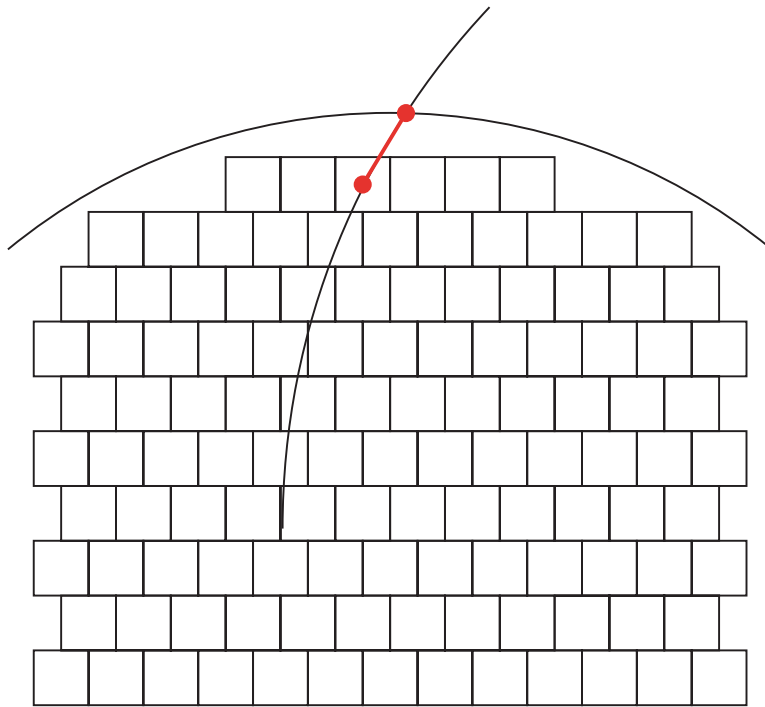
Number of kaon cells in swath= 3

Events whose number of kaon cells in swath is from 1 to 5 are corrected.  
Here are examples. If the number is larger than 5, correction isn't made.

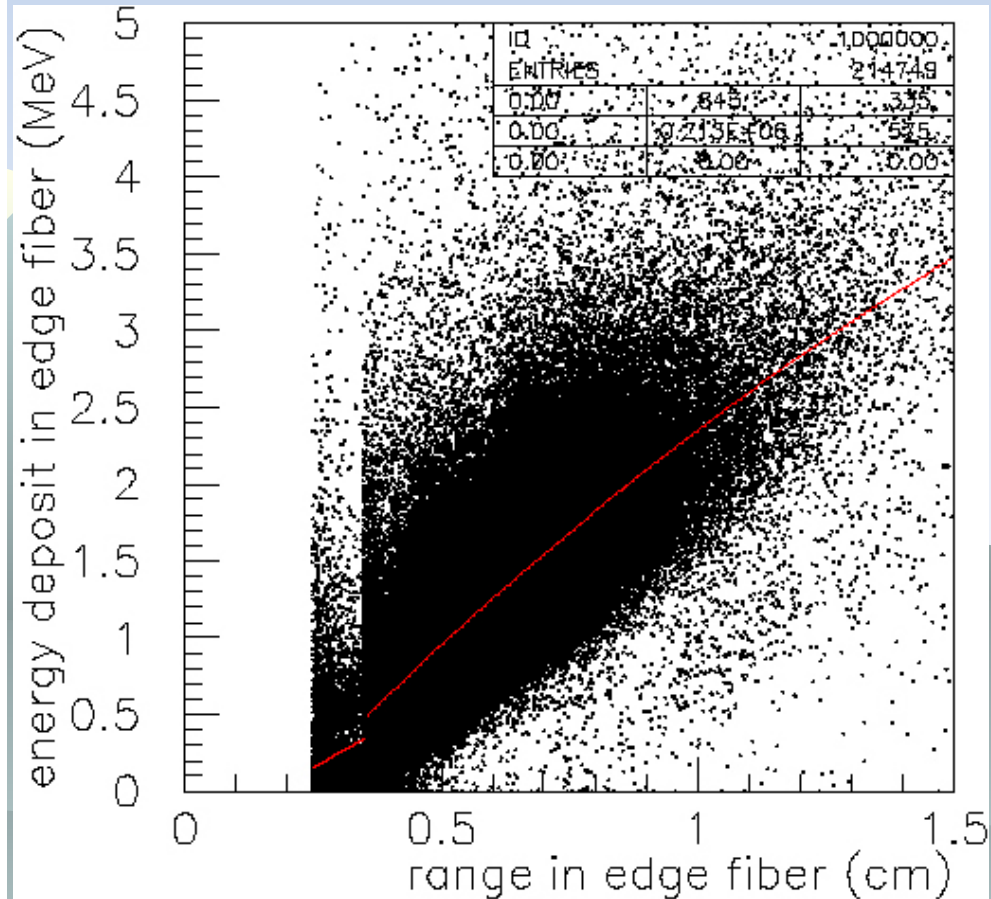


# Energy deposit in target

## energy deposit in edge fiber



TS\_D\_EDGE is length of  
red line after correction of  
dip angle



TS\_D\_EDGE

# Energy deposit in target

## Saturation effect

### Saturation effect :

Unsaturated energy – saturated energy

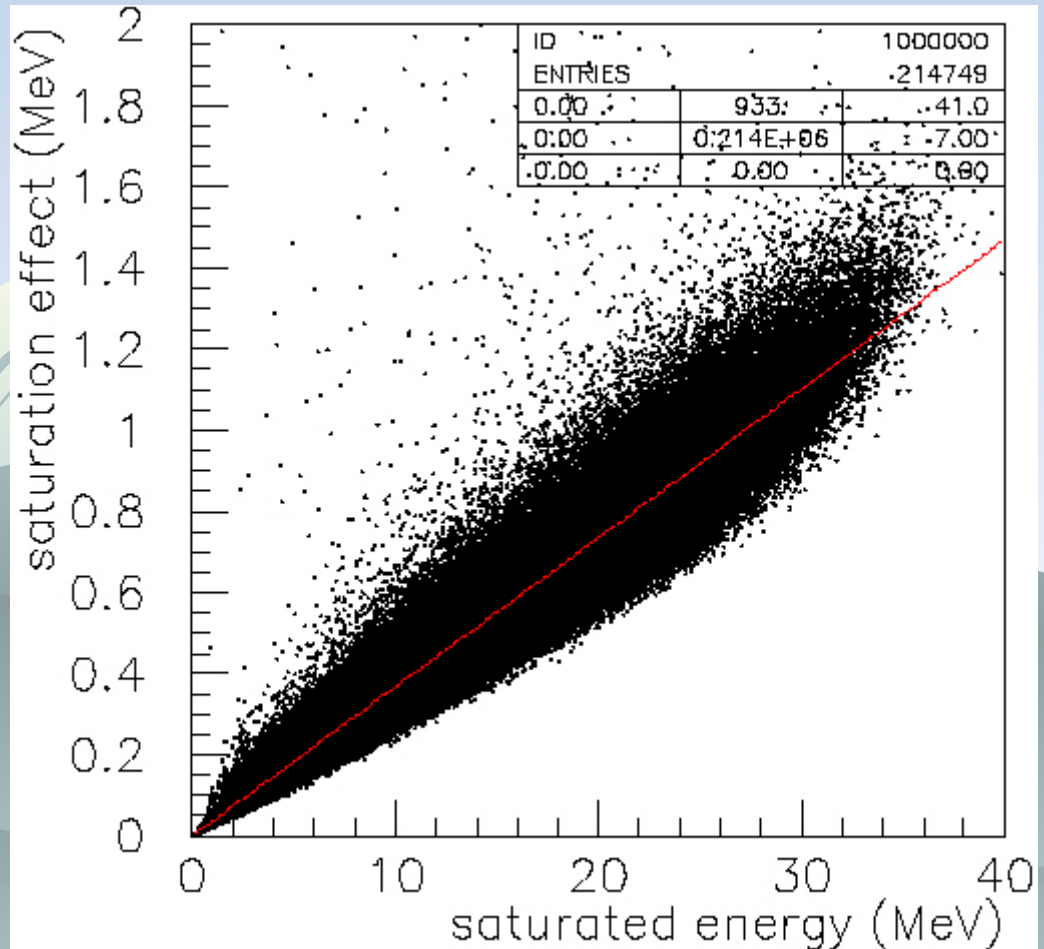
Saturation is based on birk's formula

### REAL data

Calibration on target includes saturation effect. This effect is already considered.

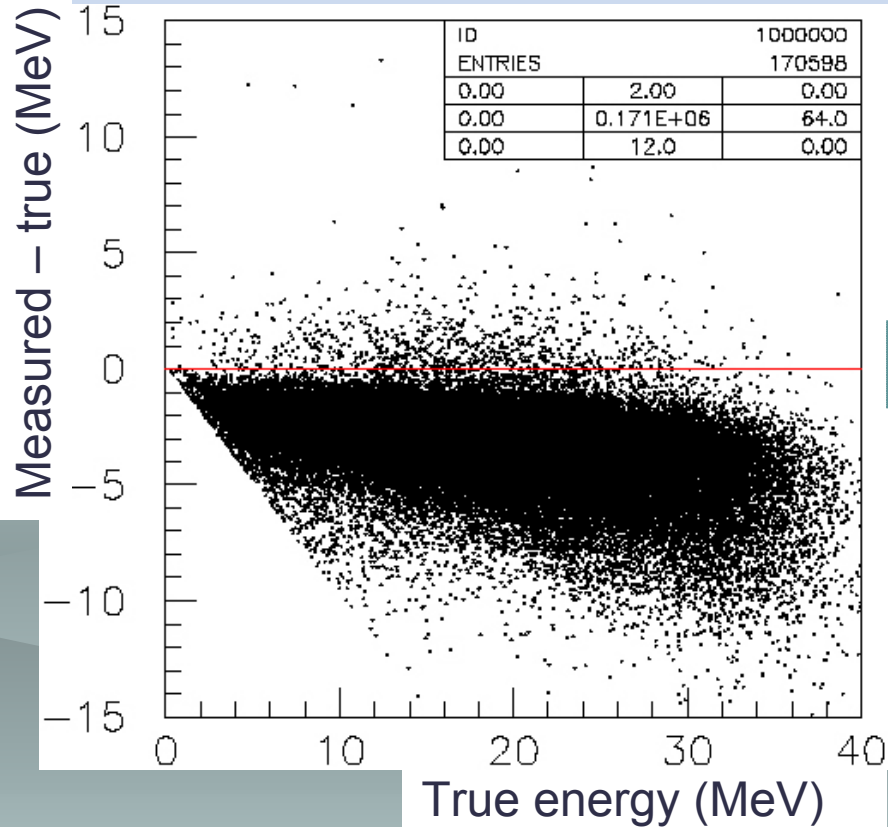
### UMC data

Saturation effect should be considered.

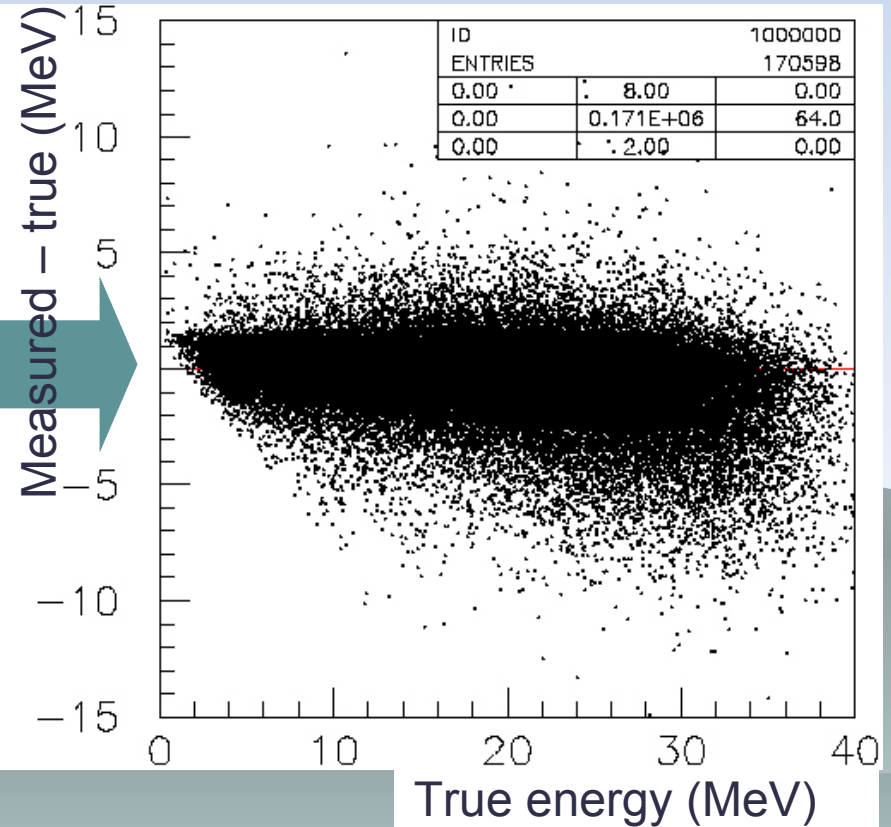


# before and after energy calibration in target

before



after



# Energy deposit in target (ETG)

Trigger 3gamma

Pion assumption

Trigger kp21

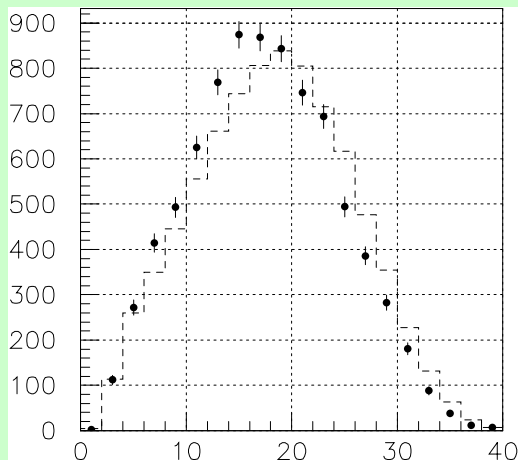
Pion assumption

Trigger km21

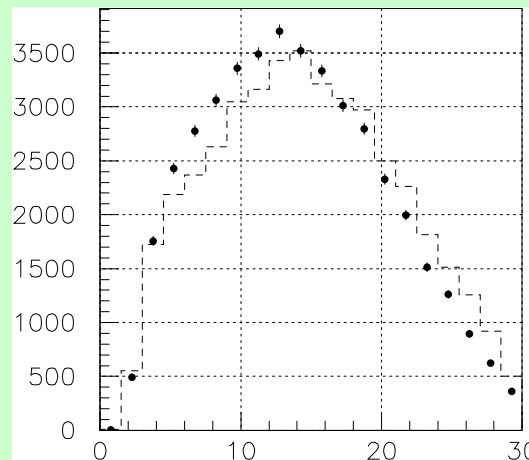
Muon assumption

OLD

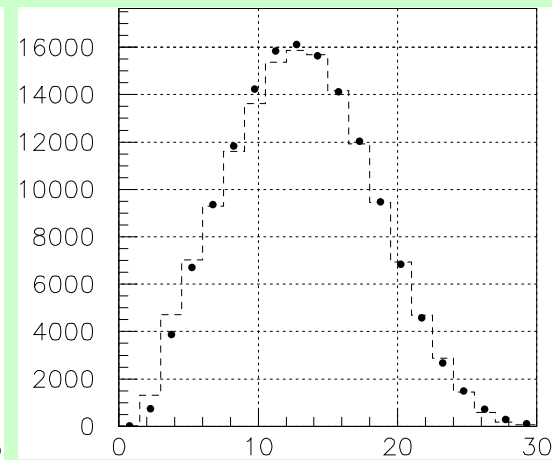
E787 standard



$\pi^+\pi^0\gamma$  MeV



$\pi^+\pi^0$  MeV



$\mu^+\nu$  MeV

NEW

After correction

# Summary of target correction

## 1) Azimuthal angle

New method is employed. Dependence on range is removed.

## 2) Range in target

A bug is fixed. Consistency of range in target is improved.

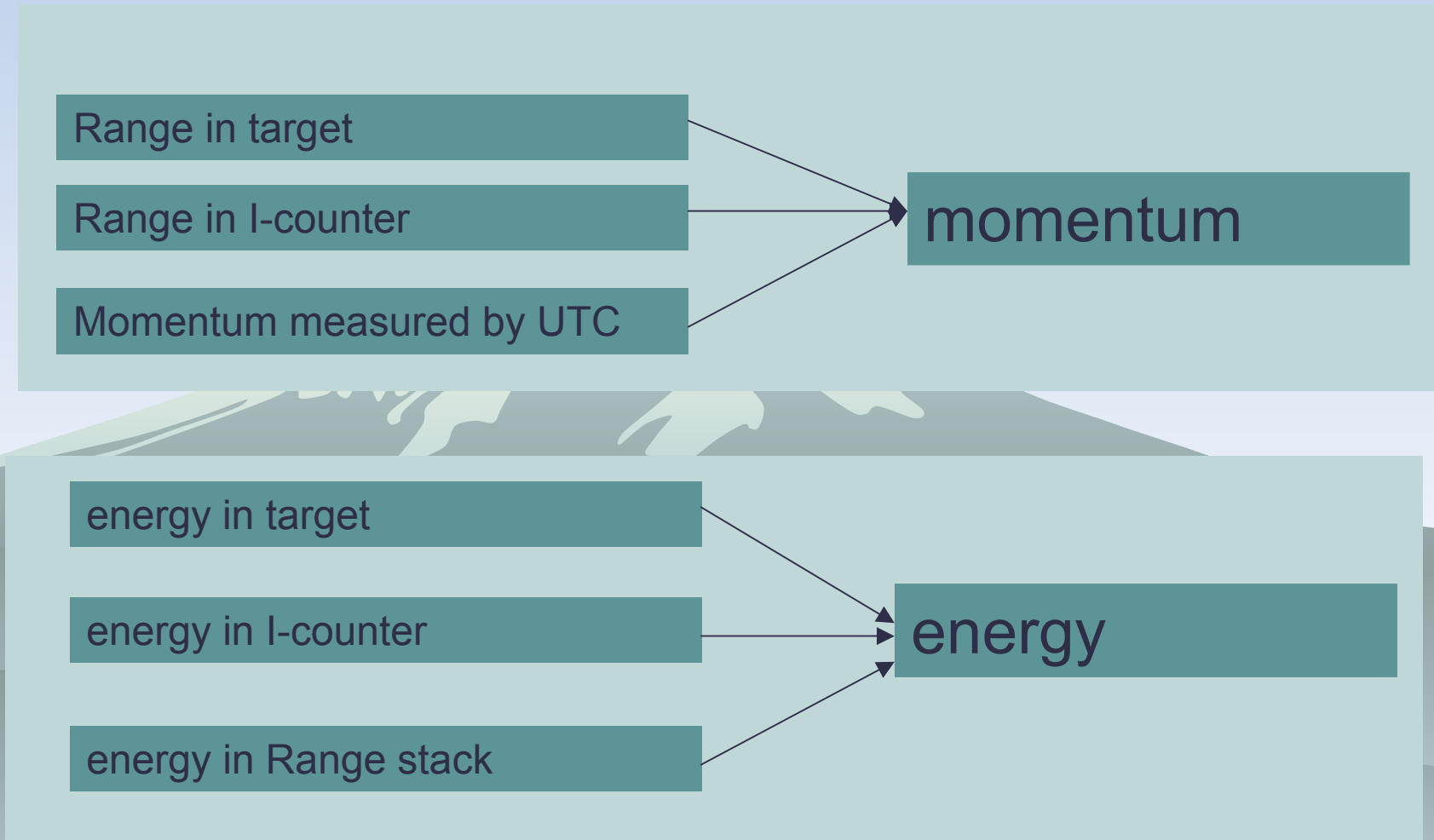
## 3) Energy deposit in target

(1) hidden energy

(2) energy deposit in edge fiber

(3) saturation effect

# Reconstruction of momentum and energy

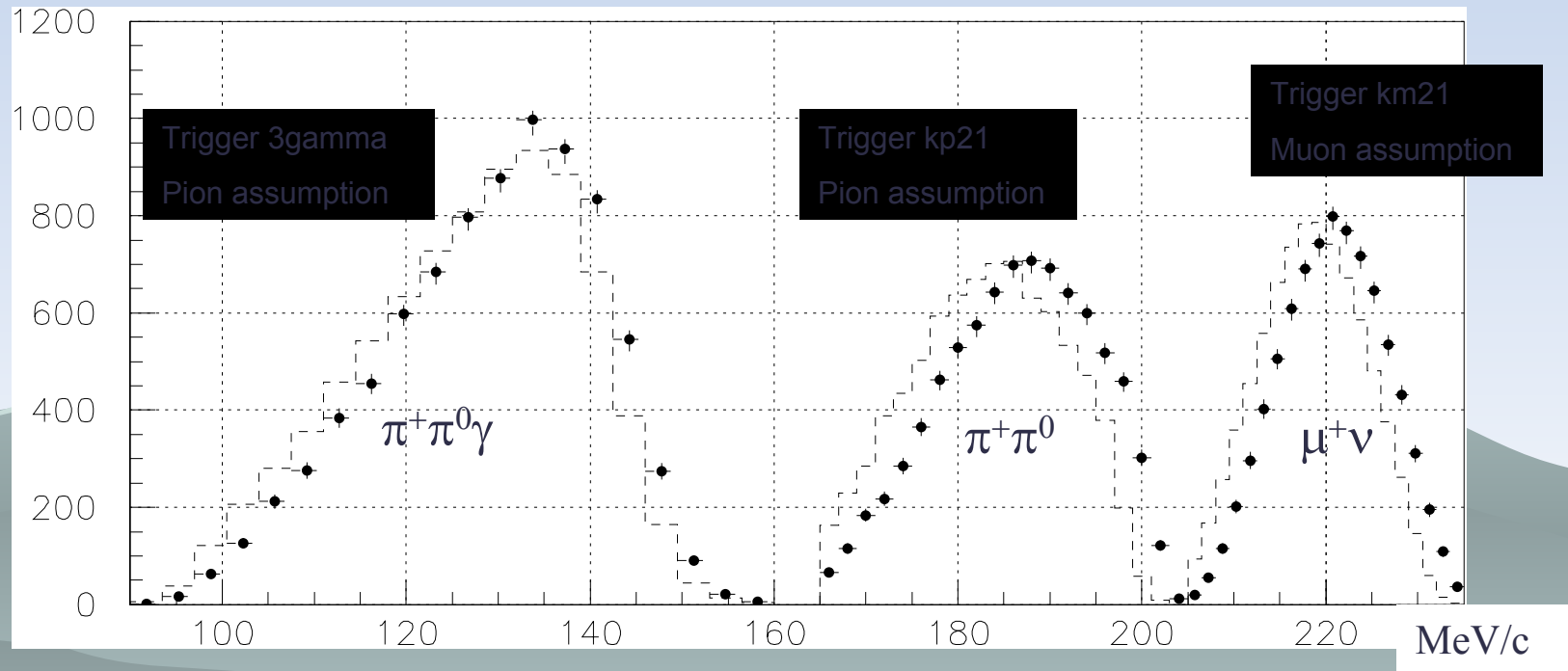


# PDC distribution in E787

(momentum measured by Drift Chamber)

• Real

----- UMC



Momentum

Distribution of PDC is different between UMC and real data

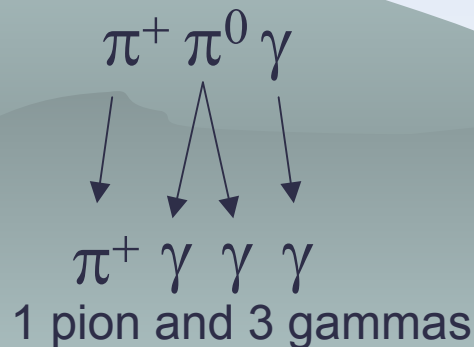
# Kinetic fit (most primary cut)

## 6 constraints

- ◆ Momentum conservation (x,y,z 3 constraints)
- ◆ Energy conservation
- ◆ mass  $\pi^+$
- ◆ mass  $\pi^0$

## 13 variables

- Pion Momentum 1
- Energy of pion and gamma 4
- Azimuthal angle 4
- Dip angle 4





# Stretch functions

Kinetic fit requires that a stretch function should be a normal Gaussian

$$\text{Stretch function} \equiv \frac{X_{meas}^i - X_{fit}^i}{\sqrt{\sigma_{meas}^i{}^2 - \sigma_{fit}^i{}^2}}$$

X: variable

$\sigma$ : resolution

There is a shift of measured variable for stretch function to be a normal Gaussian

# Shift of measured value

Stretch functions provides us the information on gap of detector position and calibration.

## UMC

Pion Momentum  $ptot' = ptot + 0.4 + 1.70 * \sigma \text{ MeV/c}$

Pion energy  $etot' = etot + 2.11 * \sigma \text{ MeV}$

Z positon of gamma no offset

$\sigma$  :Normal Gaussian  
Smearing parameter  
is set to the same  
value used  
in 1995 analysis

## Real

Pion Momentum  $ptot' = ptot - 1.4 \text{ MeV/c}$

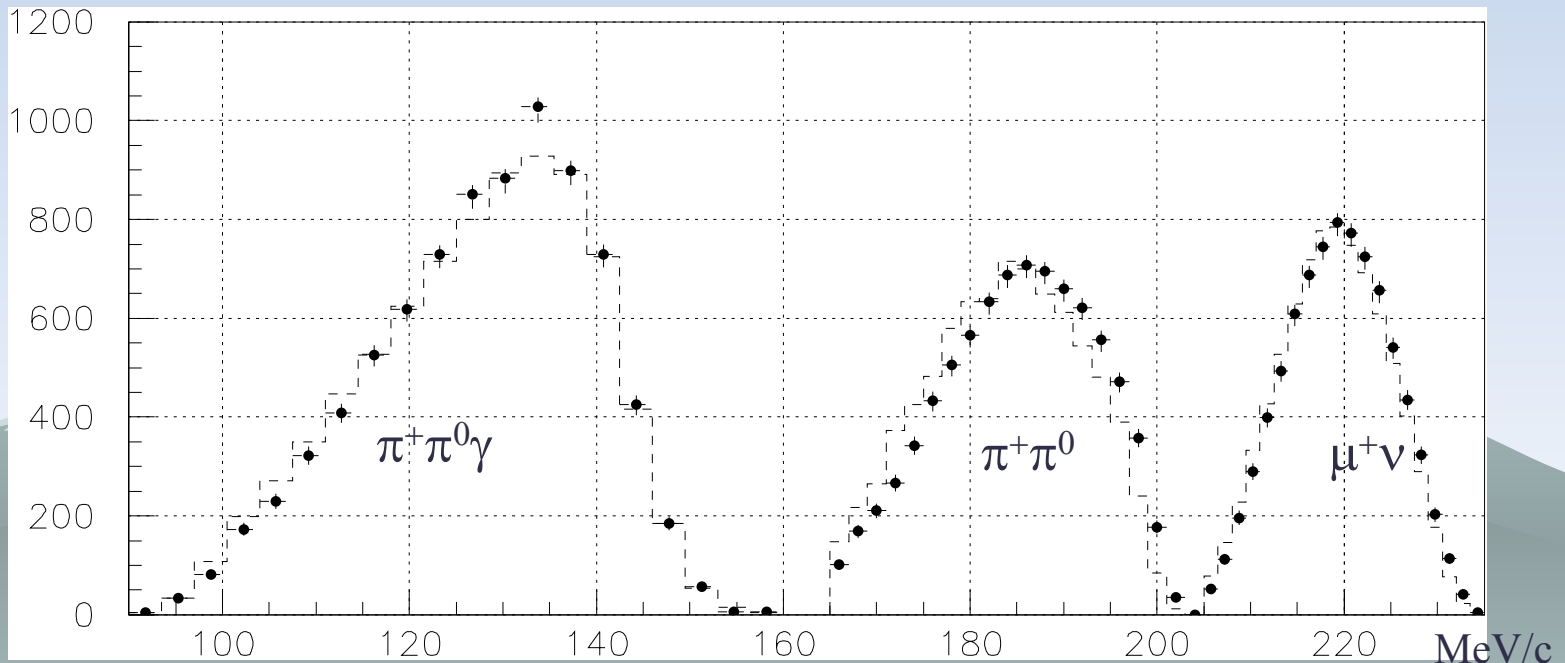
Pion energy  $etot' = etot + 1.8 \text{ MeV}$

Z positon of gamma  $ZG = ZG + 0.649 \text{ cm}$

# PDC distribution in E787

with offset (momentum measured by Drift Chamber)

• Real  
----- UMC

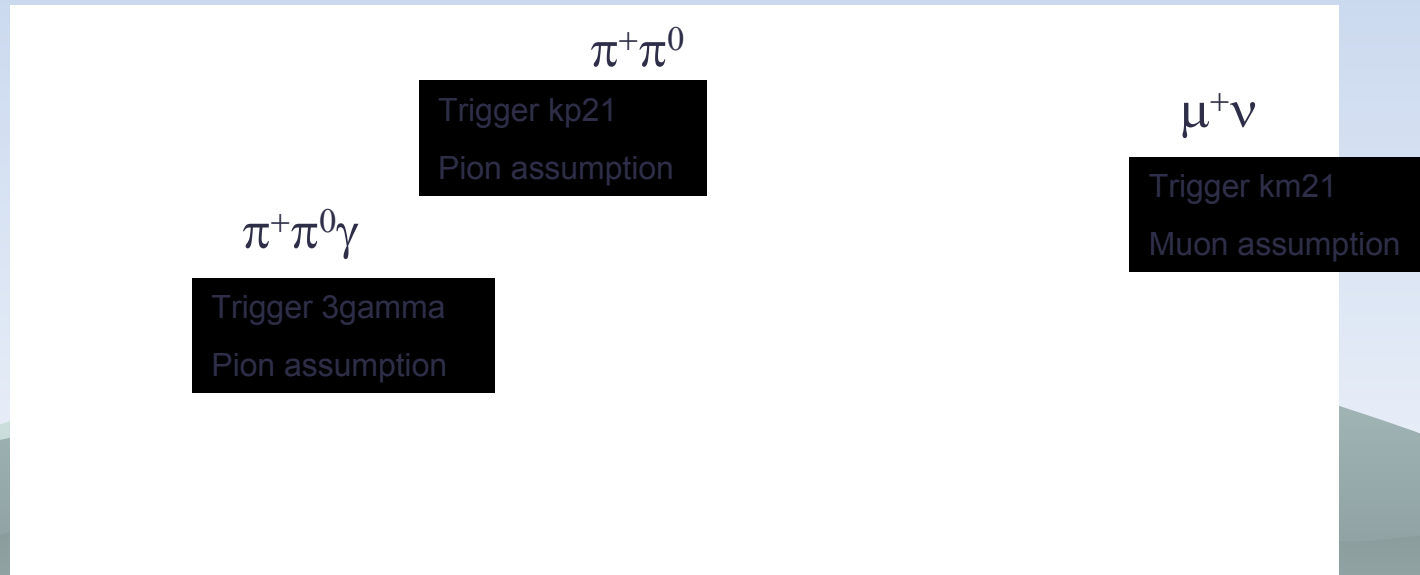


Momentum

PDC explains the discrepancy of  
momentum between real and UMC

# Momentum for kinematic fit

- Real
- UMC



input of momentum for kinetic fit

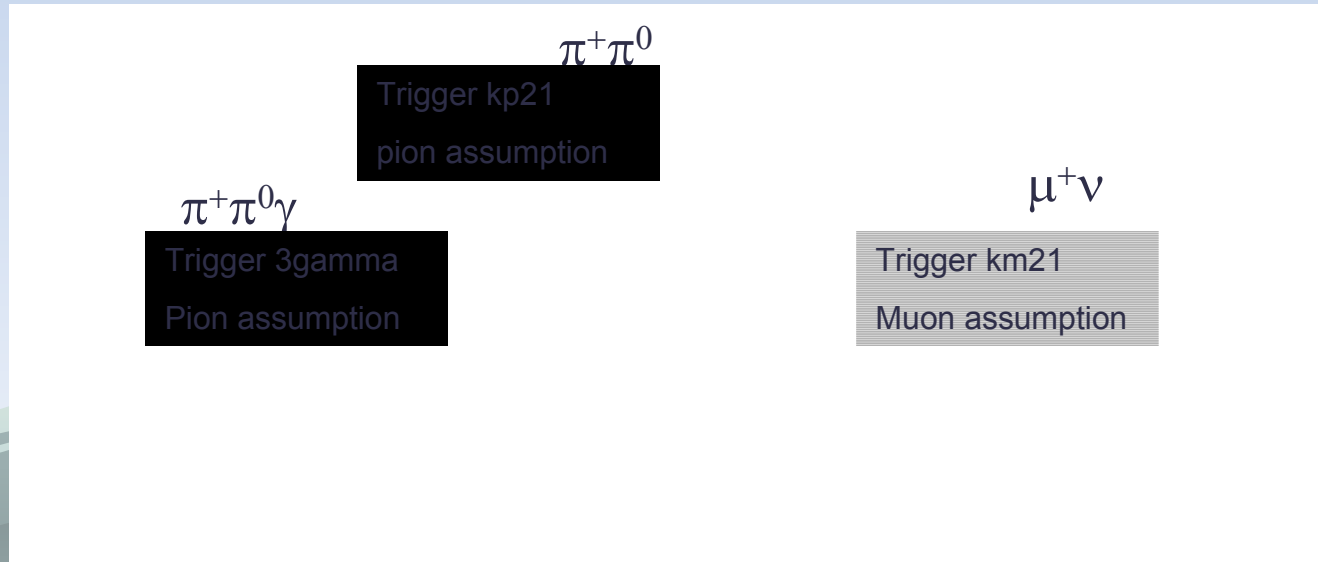
MeV/c

## Scale of momentum

Scale of momentum is consistent between UMC and real data

# Kinetic energy for kinetic fit

- Real
- UMC



Kinetic energy for input of kinetic fit MeV

Energy for kinematic fit

Scale of momentum and energy scale is different between UMC and real data

# Distribution of chisquare probability



Chisquare probability

IB



Chisquare probability

Real

Most powerful cut in this analysis

# Number of events

'98 data 1/3 sample

Number of events is **8200**  
( $140 \text{ MeV}/c < \text{pion momentum} < 180 \text{ MeV}/c$ )

# Background estimation (real data)

$$\pi^+\pi^0, \mu^+\pi^0, e^+\pi^0\nu$$

(Accidental hits)

These backgrounds are tagged by offtime photon

Tagged 755 events



$\pi^+/\mu^+$  separation

Missing momentum

kinetic fit

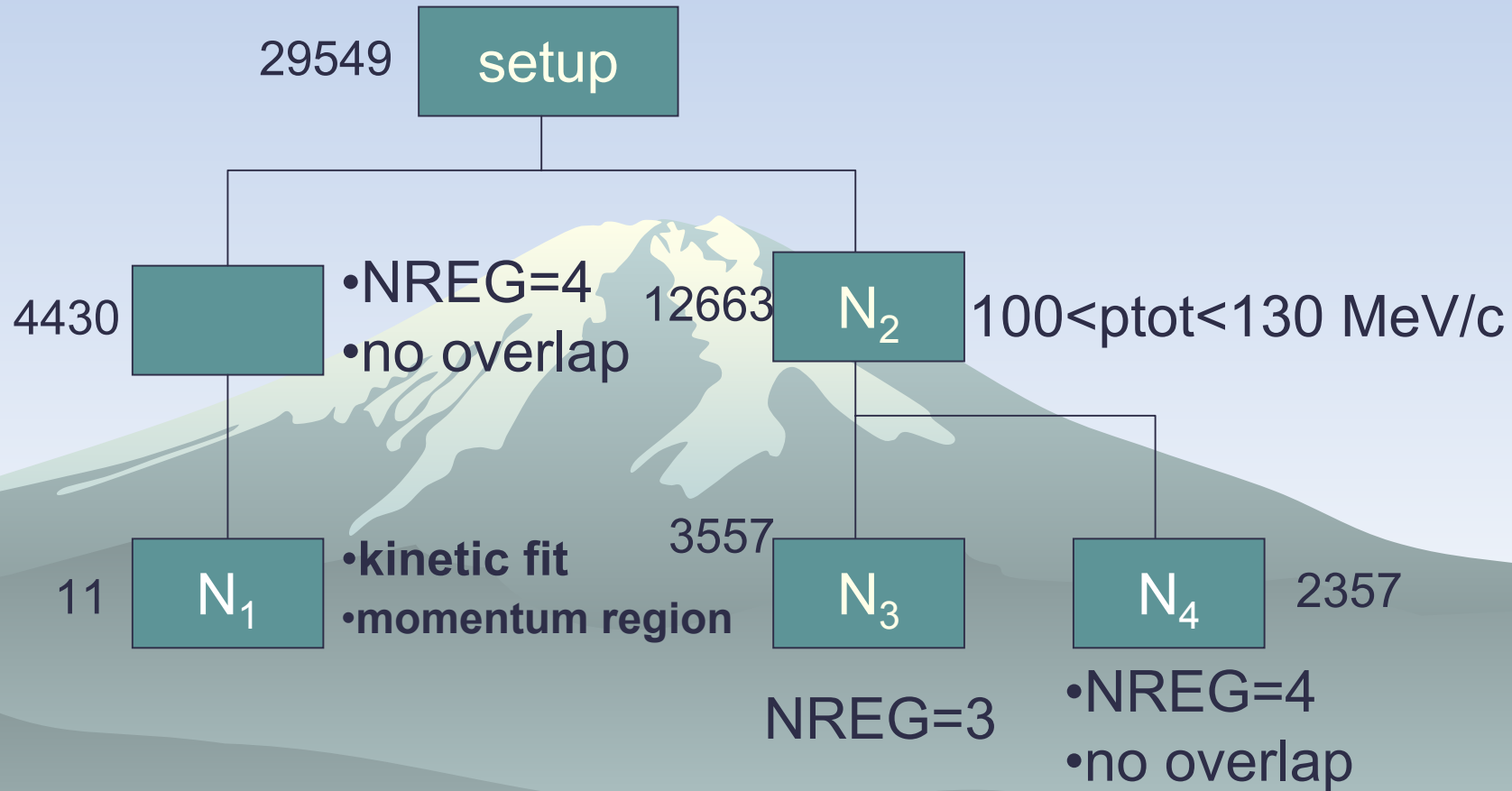


10 events remain

$$\frac{N_{\text{bkg}}}{\pi^+\pi^0\gamma} = 0.16\%$$



# $\pi^+\pi^0\pi^0$ bifurcation



$$N_{bkg} = \frac{N_1}{N_4} \times \frac{1}{N_2} = \frac{N_1 \times N_3}{N_4} = 7.3 \text{ events}$$

$$\frac{N_{bkg}}{\pi^+\pi^0\gamma} = 0.11 \%$$

# Summary of background estimation

$\pi^+\pi^0, \mu^+\pi^0, e^+\pi^0\nu$  0.16%  
(Accidental hits)

$\pi^+\pi^0\pi^0$  0.11%

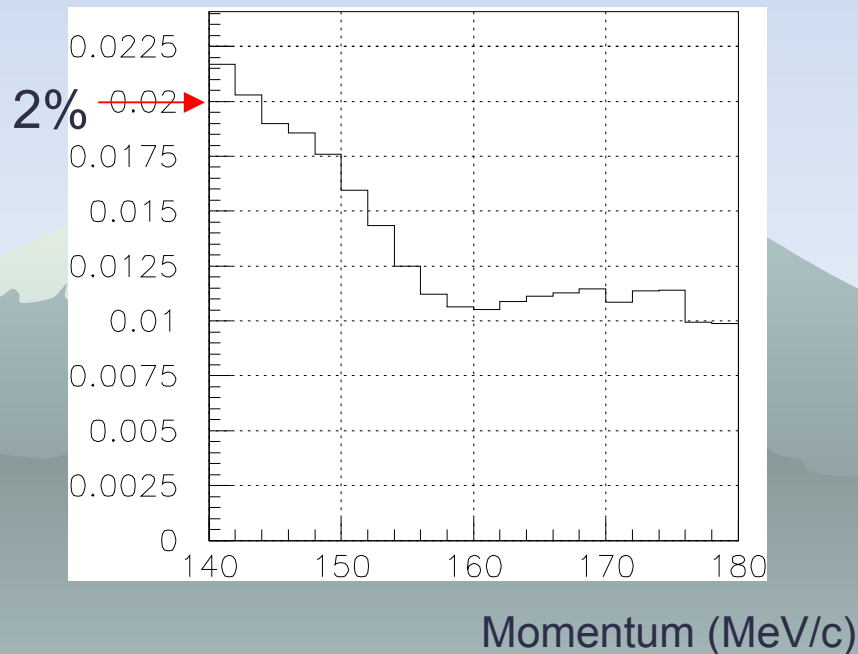
Background estimation

**Background level is low.**

140 MeV/c < pion momentum < 180 MeV/c

# Real data & UMC consistency

Events are rejected if  $W$  is larger than 0.4 in order to make more pure IB sample.



DE component is negligible if  $W < 0.4$

Ratio of DE to IB if  $BR(DE)$  is assumed to  $4.7 \cdot 10^{-6}$

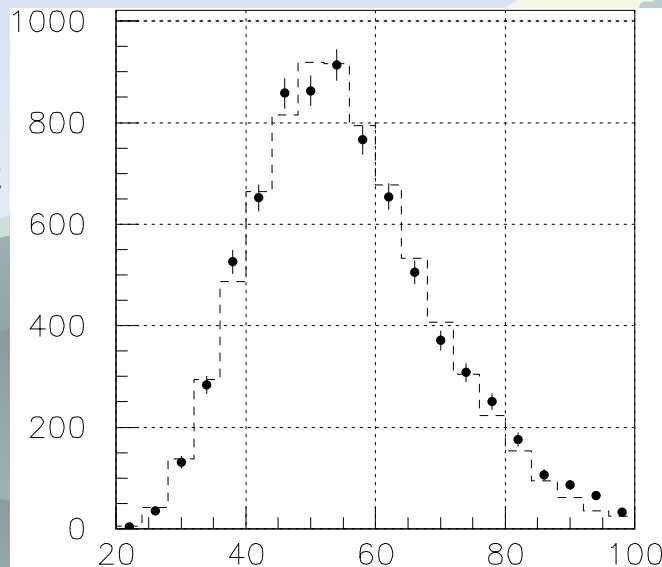
# Real data & UMC consistency

UMC IB data reproduces the real data?

Events are rejected if  $W$  is larger than 0.4 in order to make more pure IB sample.

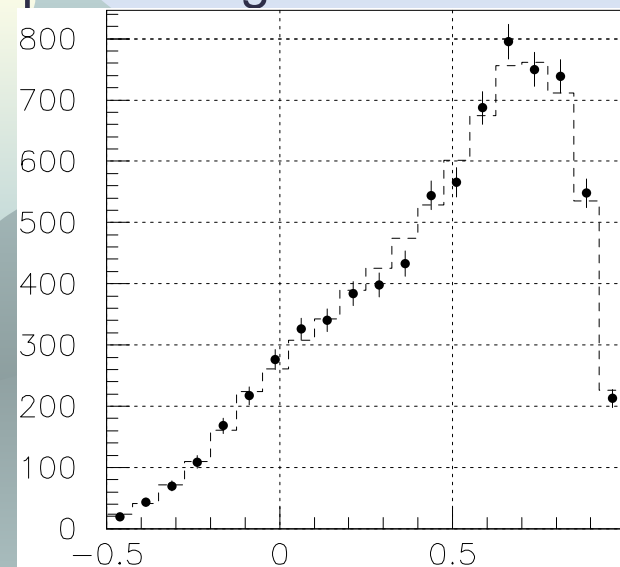
Gamma energy

• Real  
----- UMC



MeV

Opening angle between  
pion and gamma



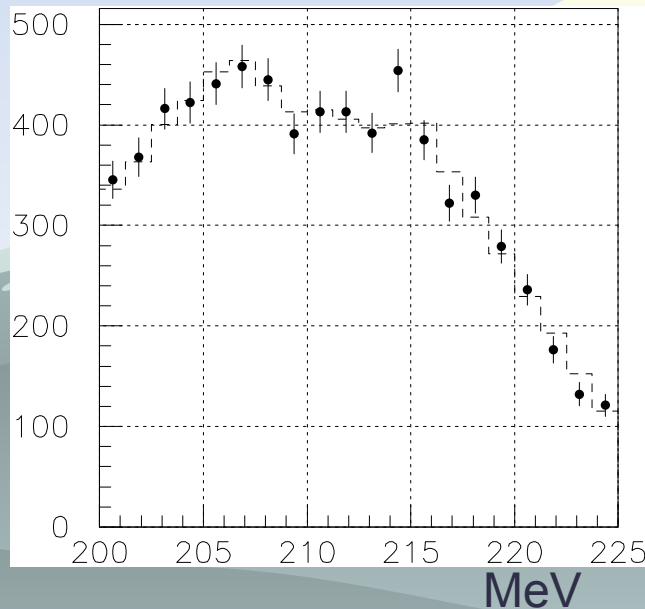
cos

# Real data & UMC consistency

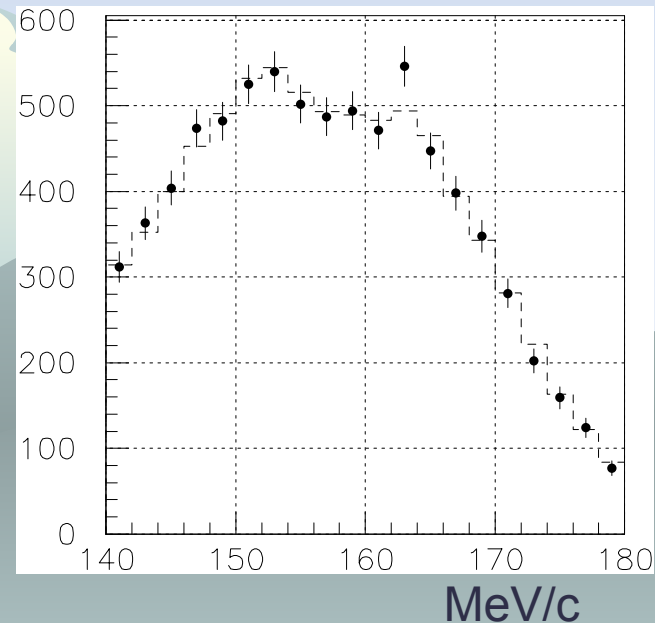
UMC IB data reproduces the real data?

Events are rejected if  $W$  is larger than 0.4 in order to make more pure IB sample.

Pion total energy



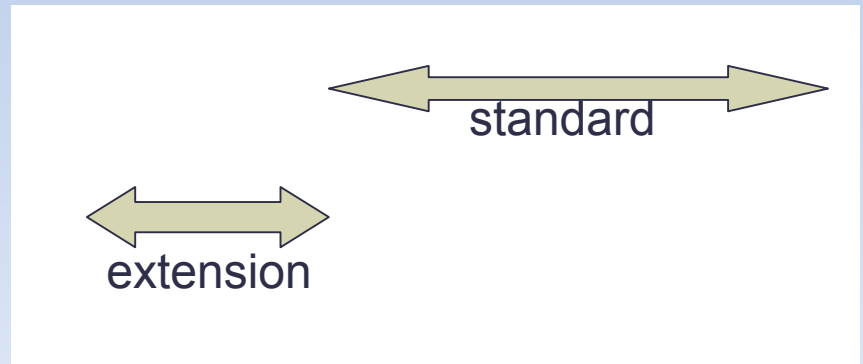
Pion momentum



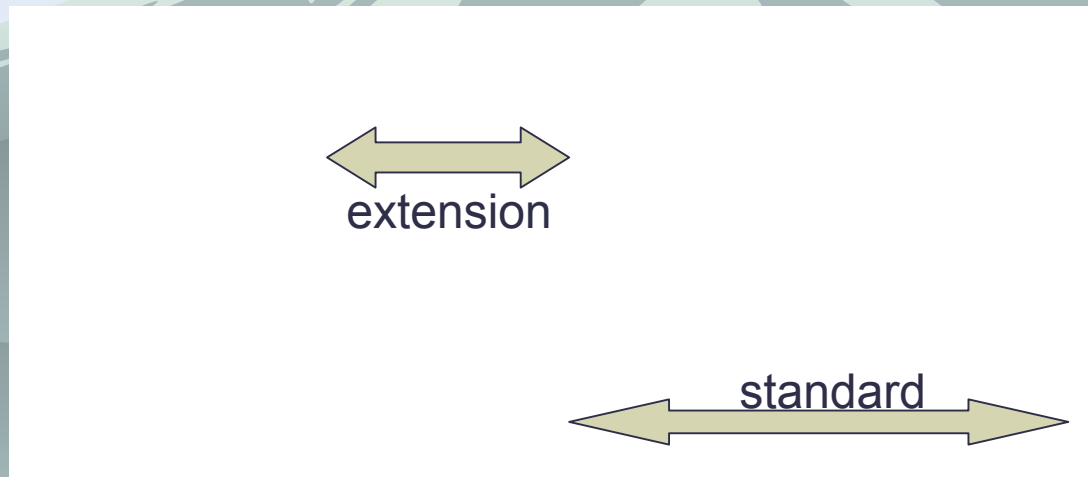
# Extension to lower momentum region

IB/DE ratio

Assuming  
 $BR(DE)=4.7 \cdot 10^{-6}$



Momentum (MeV/c)



Assuming that the ratio of IB/DE  
in  $140 \text{ MeV/c} < P < 180$  is the  
same in lower momentum region

Momentum (MeV/c)

- Real
- UMC(IB)

# Summary and future prospect

- ◆ Correction on target is done
- ◆ Consistency between real and UMC is retained.
- ◆ Study of lower momentum region